



EXAMINATIONS — 2002

END-YEAR

COMP 307

Model Answers

Time Allowed: 3 Hours

Instructions: There are a total of 180 marks on this exam.
Attempt all questions.
Calculators may be used.
Non-electronic foreign language translation dictionaries may be used.

Questions

- | | |
|---------------------------------------|------|
| 1. Prolog | [25] |
| 2. Search | [20] |
| 3. State Space Problem solving | [20] |
| 4. Rule Based Systems | [20] |
| 5. Machine Learning | [25] |
| 6. Planning | [25] |
| 7. Natural Language Processing. | [25] |
| 8. Artificial Intelligence and Chess. | [20] |

Question 1. Prolog

[25 marks]

(a) [6 marks] For each of the queries below, state the answer that prolog would give (“yes”, “no”, or a variable binding).

For example,

```
|?- a = a.           yes
|?- 4 = 2+3.        no
|?- [a, b] = [X, b]. X=a
```

```
|?- X=isa(c1, cup). X=isa(c1, cup)
|?- X = 5+3. X=5+3
|?- X is 5+3. X=8
|?- X=5, X is X+3. no
|?- first \== second. yes
|?- att(cup1, X)= att(Y, white). X=white, Y=cup1.
|?- att(cup1, X)= att(X, white). no.
|?- [cup, bench, kitchen] = [X | Y]. X=cup, Y=[bench,
kitchen]
|?- [c1, on(Y, Z), in(b, k)] = [X, on(X, b) | W].
X=c1, Y=c1, Z=b, W=[in(b, k)]
```

Consider the following prolog program.

```
in(p0, kitchen).
in(c1, diningroom).
in(c2, kitchen).
in(c3, kitchen).
in(c4, kitchen).

plate(p0).
cup(c1).
cup(c2).
cup(c3).
cup(c4).

clean(p0).
dirty(c1).
clean(c2).
dirty(c3).
clean(c4).

toWash(X):-in(X, kitchen), format("~n In: ~w", [X]),
cup(X), format("~n Cup: ~w", [X]),
dirty(X), format("~n Dirty: ~w", [X]),
fail.
```

(b) [6 marks] What is the output of the following query?

```
|?- toWash(X).
```

```
In: p0
In: c2
Cup: c2
In: c3
Cup: c3
Dirty: c3
In: c4
Cup: c4
no
```

(c) [3 marks] Suppose a cut were added to the toWash predicate (on the second line):

```
toWash(X):-in(X, kitchen), format("~n In: ~w", [X]),
           cup(X),          format("~n Cup: ~w", [X]), !,
           dirty(X),        format("~n Dirty: ~w",[X]), fail.
```

What would the output of the following query be?

```
|?- toWash(X).
```

```
In: p0
In: c2
Cup: c2
no
```

(d) [10 marks].

Write a predicate, relevantTo(X, L, L2), where L is a list of terms and L2 is a sublist of L containing just the terms that have X as their first argument. For example,

```
|?- relevantTo(c1, [on(c1, bench), on(c2, table), china(c1),
                   isa(c2, cup), att(c1, colour, white)], Z).
```

```
Z = [on(c1, bench), china(c1), att(c1, colour, white)]
```

You will need to use the operator =.. that “deconstructs” a term into a list of the head and arguments of the term:

```
|?- in(c2,kitchen) =.. X.
X = [in, c2, kitchen]
```

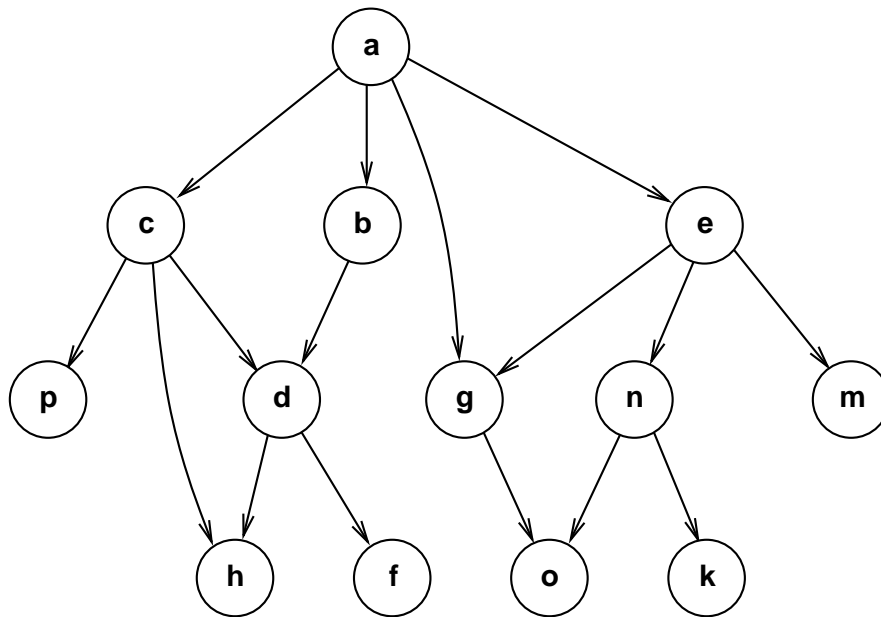
```
relevantTo(X, [], []).
relevantTo(X, [H|T], [H|R]) :-
    H =.. [_ , X | _],
    relevantTo(X, T, R).

relevantTo(X, [H|T], R) :-
    relevantTo(X, T, R).
```

Question 2. Search

[20 marks]

(a) [8 marks] Consider the following state space, where each node represents a state, and each directed link represents an operation.



Suppose the state space is to be searched, starting at node “a”. List the nodes of the state space in the order that they are expanded for each of the following search methods. Assume that the search considers child nodes from left to right. State any other assumptions you make.

Depth First Search:

a, c, p, h, d, f, b, g, o, e, n, k, m. (Assume mark and don't revisit nodes)
OR: a, c, p, h, d, h, f, b, d, h, f, g, o, e, g, o, n, o, k, m. (Assume don't mark nodes)

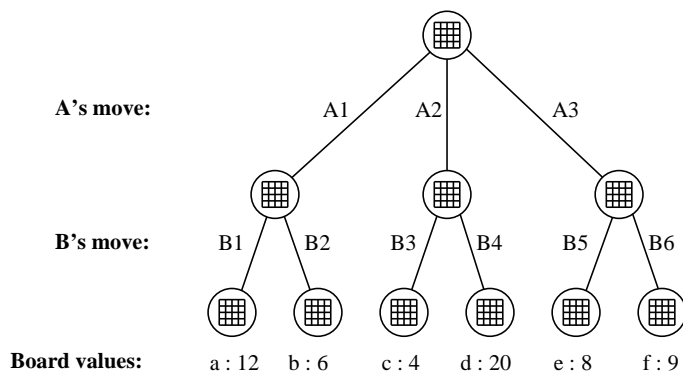
Breadth First Search:

a, c, b, g, e, p, h, d, o, n, m, f, k. (Assume mark and don't revisit nodes)
OR: a, c, b, g, e, p, h, d, o, g, n, m, h, f, o, k. (Assume don't mark nodes)

Iterative Deepening:

a, c, b, g, e,
a, c, p, h, d, b, g, o, e, n, m,
a, c, p, h, d, f, b, g, o, e, n, k, m,

Consider the following tree of board positions from a two person board game like chess. The tree shows that player A has three possible moves from the current board position and player B has two possible moves from each of the resulting positions. The values of the board positions after each of B's moves are shown at the bottom (larger numbers are better for A).



(b) [3 marks] Which move should player A make, and why?

move A3, because the lowest possible outcome is 8, which is higher than the lowest possible outcome for A1 (6) or A2 (4).

(c) [3 marks] If evaluating board positions is expensive, we want to avoid evaluating any board unless necessary. Which board position(s) from “a” to “f” do not need to be evaluated to determine the best move for A? Explain why.

Don't need to evaluate board "d". After evaluating "c" we know that if player A takes move A2, A will get at most 4. Since A can get at least 5 by taking move A1, move A2 is clearly not the best move, and there is no need to find out anything more about it.

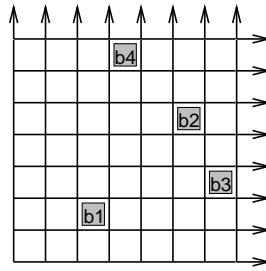
(d) [6 marks] Depth First, Hill Climbing, and A* search use different stopping criteria. State the stopping criteria for each kind of search and briefly indicate what class of search problem they are appropriate for.

DFS: stop when reach goal state. Appropriate when problem requires any goal state or any path to a goal state.
 Hill Climbing: stop when all neighbours of current best node are worse than current node. Appropriate when problem requires an optimal state, but can't tell from state whether it is the best or not.
 A*: stop when have a path to a goal state and all other paths have higher estimated cost than than this path. Appropriate when problem requires an optimal path to a goal state and can determine whether a state is a goal state.

Question 3. State Space Problem Solving

[20 marks]

Consider a robot in a world consisting of a collection of labeled boxes that can each be placed in any square of an infinite grid (at most one block per grid square). At each step, the robot can push one box by one step in any direction (N, S, E, W).



A state in the state space can be specified by giving a location (x,y) for each box (assume four boxes):
`state(b1(3,2), b2(6,5), b3(7,3), b4(4,7))`

The possible actions could be specified by the box and the direction:
`move(b1, N), move(b1, S), move(b1, E), move(b1, W)`
`move(b2, N), move(b2, S), etc`

If the robot were given initial and final states:
 initial: `state(b1(3,2), b2(6,5), b3(7,3), b4(4,7))`
 final: `state(b1(13,2), b2(6,15), b3(7,1), b4(1,1))`—

the robot could search for a sequence of moves to get from the initial state to the final state.

(a) [3 marks] Show the first three states that the robot might consider if it used depth first search:

`state(b1(3,3), b2(6,5), b3(7,3), b4(3,7))`
`state(b1(3,4), b2(6,5), b3(7,3), b4(3,7))`
`state(b1(3,5), b2(6,5), b3(7,3), b4(3,7))`

(b) [3 marks] Why would depth first search be a very bad strategy for the robot?

Because it could search forever moving the first block North, never getting closer to the goal, and never trying any other path.

(c) [3 marks] Breadth first search would be a better strategy. Why is it still not a good strategy?

Because it is expensive, requiring very large amount of memory.
 The number of nodes in the queue = $O(30^{16})$,

(d) [3 marks] Why would iterative deepening be a better strategy than breadth first?

Like BFS, it doesn't get stuck going down one path, but it doesn't use nearly as much memory as BFS (However, it will take just as long)

(e) [8 marks] Suggest a heuristic that would make A* search a reasonable search strategy for this problem domain. Explain why your heuristic is admissible.

heuristic = sum of the distances of each block from their goal position, (add to the number of steps on the current path (depth of node) to get the value of a node).
 The distances should be Manhattan distance — the number of steps along the grid to the goal, not the Euclidean distance.
 $\sum_{i=1}^4 (|x_i - u_i| + |y_i - v_i|)$ where x_i, y_i is the current position of the i th block, and u_i, v_i is its goal position.
 This is guaranteed to be a lower bound on the actual distance (hence admissible) because the blocks will take at least this many steps. If they get in the way of each other, the distance may be greater, so it is not a perfect heuristic

Question 4. Rule Based Systems

[20 marks]

Consider the following set of rules for a rule based system for determining whether there is oil at a location on the basis of various geological features.

- | | |
|--|------------------------------|
| 1. If <u>alkalite</u> and high watertable | then fold morphology |
| 2. If <u>quartz</u> | then fold morphology |
| 3. If <u>shale</u> and <u>crystallite</u> | then slope morphology |
| 4. If <u>schist</u> and alkalite | then slope morphology |
| 5. If fold morphology and low chryolation | then deep oil |
| 6. If fold morphology and calcification | then shallow oil |
| 7. If slope morphology and <u>moraine-transfer</u> | then deep oil |
| 8. If slope morphology and sinkage | then no oil |

Suppose we were to use a backward chaining inference system that cached answers and intermediate conclusions and considered the three hypotheses in order:

shallow oil, deep oil, no oil

Suppose also that when asked about a fact, the user would give the following answers: (note, the true facts are also underlined in the rules above)

- | | |
|----------------------------|-----|
| A. alkalite | no |
| B. calcification | no |
| C. low chryolation | no |
| D. <u>crystallite</u> | yes |
| E. <u>moraine-transfer</u> | yes |
| F. quartz | yes |
| G. schist | yes |
| H. shale | yes |
| I. sinkage | no |
| J. high watertable | no |

(a) [5 marks] Show the sequence of rules the inference engine would consider.

6, 1, 2, 5, 7, 3

(b) [4 marks] Show the sequence of facts it would ask about.

alkalite, quartz, calcification, low chryolation, shale,
crystallite, moraine-transfer

(c) [1 mark] State which hypothesis it would conclude.

deep oil

(d) [4 marks] What explanation might the system give if asked to justify its conclusion?

deep oil by rule 7,
and slope morphology by rule 3,

(b) [4 marks] State the desirable properties for an “impurity measure” on a set of instances, and give an example of an acceptable impurity measure.

Should be 0 if all instances are the same class
 Should be a maximum if equal numbers of instances of each class
 Should be smooth

Consider the following data set describing 10 kinds of mushrooms of which 5 are poisonous and 5 are safe. They are described by three attributes.

Colour	Stalk	Top	Class
red	tapered	flat	Poisonous
red	tapered	round	Poisonous
red	bulbous	round	Poisonous
brown	bulbous	round	Poisonous
brown	bulbous	round	Poisonous
brown	tapered	round	Safe
brown	tapered	round	Safe
white	tapered	round	Safe
white	bulbous	round	Safe
white	bulbous	flat	Safe

(c) [6 marks] Which attribute would the decision tree building algorithm choose for the root of the decision tree? Show your working and state which impurity measure you are using.

Impurity measure $\text{prob}(\text{Poisonous}) * \text{prob}(\text{Safe})$
 Colour: $0 + 0.4 * 0.25 + 0 = 0.1$
 Stalk: $3/5 * 2/5 = 6/25 = 0.24$
 Top: $0.8 * 0.25 + 0.2 * 0.25 = 0.25$
 Therefore, chooses the Colour attribute

(d) [5 marks] A perceptron is a linear weighted threshold device. It has several (numeric) inputs and a boolean output. If the input values of a perceptron are represented by the variables x_1, x_2, \dots, x_k , give the formula for computing the output of the perceptron. Explain any variables you use other than x_i .

output = true if $\sum_{i=1}^k w_i x_i > \theta$
 = false otherwise
 w_i are the weights
 θ is the threshold value

(e) [5 marks] Very briefly outline the algorithm for learning the weights of a perceptron from a set of examples (eg, the mushroom data on the previous page). You do not have to specify exactly how the weights are modified.

Repeatedly present an instance to the perceptron
 if positive instance and wrong, then add instance to the weights
 if negative instance and wrong, then subtract instance from weights
 else, do nothing

Question 6. Planning

[25 marks]

(a) [4 marks] What are the four parts of a STRIPS operator?

```
name and parameters
Preconditions
Adds: facts added by the operation
Deletes: facts deleted by the operation
```

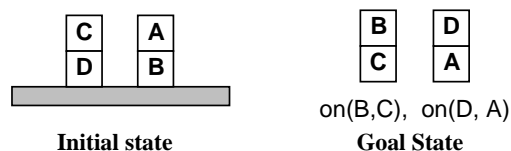
(b) [4 marks] Write a STRIPS operator for the action `paint`. To paint an object a particular colour, the robot must be holding a paint brush of the right colour. The effect of the action is to change the colour of the object.

```
paint( obj, newColour, brush, oldColour)
pre:  hold(brush), colour(brush, newColour)
      colour(obj,oldColour)
del:  colour(obj, oldColour)
add:  colour(brush, newColour)
```

(c) [4 marks] STRIPS operators are very limited in the kinds of actions that they can represent. List at least four properties of actions for real world robots that cannot be easily represented in standard STRIPS operators,

```
duration: STRIPS actions are assumed to act in discrete time.
conditional effects: STRIPS operators have no conditions.
resources: can't represent the continuous amounts of resources
concurrent actions: STRIPS actions are instantaneous.
disjunctive preconditions: must be conjunction
guarded actions
sensing actions
```

(d) [6 marks] Explain why a goal-stack planner would have difficulty finding a good solution to the following blocks world problem? (Assume the “standard” operators of pickup, putdown, stack, and unstack.)



Because it tries to solve the subgoals independently. If it tried to achieve $\text{on}(B, C)$ first, it would remove A, then put B on top of C while it was on top of D. It would then have to undo $\text{on}(B, C)$ in order to put $\text{on}(D, A)$ and then redo $\text{on}(B, C)$.

If it tried to achieve $\text{on}(D, A)$ first, it would do the same thing (put D on A on B, and then have to undo $\text{on}(D, A)$ to achieve $\text{on}(B, C)$)

Suppose we are using a Partial Order Planner (POP) to construct a plan for a meal of fried eggs in a dish. The diagram below shows the state of the plan after the planner has added three new actions to satisfy some of the preconditions.

(e) [4 marks] The last action added has introduced two threats into the plan. Identify the threats on the plan and show two different ways to resolve them.

pp --> prep, np.	lexicon(plate, noun).
	lexicon(bench, noun).
	lexicon(kitchen, noun).
np --> det, np1.	
	lexicon(take, verb).
np1 --> adj, np1.	lexicon(get, verb).
np1 --> noun, np1.	lexicon(put, verb).
np1 --> noun.	lexicon(place, verb).
prep --> [P], {lexicon(P, prep)}.	lexicon(white, adj).
det --> [D], {lexicon(D, det)}.	lexicon(blue, adj).
noun --> [N], {lexicon(N, noun)}.	
verb --> [V], {lexicon(V, verb)}.	lexicon(to, prep).
adj --> [A], {lexicon(A, adj)}.	lexicon(from, prep).
	lexicon(on, prep).
	lexicon(in, prep).
	lexicon(the, det).
	lexicon(a, det).

(a) [4 marks] Show the parse tree for the command

“take the plate to the kitchen”

```
s(verb(go),
  pp(prepare(to),
    np(det(the),
      np1(noun(kitchen))))))
```

(b) [3 marks] Show the parse tree for the command

“put a white cup on the kitchen bench”

```
s(verb(put),
  np(det(a),
    np1(adj(white),
      np1(noun(cup))))),
  pp(prepare(on),
    np(det(the),
      np1(noun(kitchen),
        np1(noun(bench))))))
```

(c) [3 marks] Why can't the grammar parse the sentence

“place the blue plate on the cup in the kitchen”

the grammar only allows one PP in the sentence, (and none in the NP). This sentence has two PP's (“on the cup” and “in the kitchen”). Therefore, the second PP can't be parsed.

(d) [4 marks] Replace the rule for np by a rule or rules that let the grammar also correctly parse the sentence

“place the blue plate on the cup in the kitchen”

```
np --> det np1.  
np --> det np1 pp.  
note that this does not allow multiple PP's on an NP  
That would be permissible, but not required
```

(e) [11 marks] The original grammar is too general – it allows invalid sentences, like the two on the left below, although the two on the right are valid.

“*take the cup on the kitchen”

“take the cup to the kitchen”

“*put the plate to the bench”

“put the plate on the bench”

The problem is that the preposition in the PP doesn't match the verb:

- The verbs “take” and “get” must have a PP with a location-specifying preposition: “to” or “from”.
- The verbs “put” and “place” must have a PP with an object-specifying preposition: “on” or “in”.

Extend the grammar and the lexicon to enforce the constraint that the preposition matches the verb. You will need to modify some rules and the lexicon, but you do not need to add any new grammar rules. You do not need to modify the lexicon entries for nouns, adjectives, or determiners.

```
s --> verb(Cat), np, pp(Cat).  
pp(Cat) --> prep(Cat), np.  
np --> det, np1.  
np1 --> adj, np1.  
np1 --> noun, np1.  
np1 --> noun.  
prep(Cat) --> [P], lexicon(P, prep, Cat).  
det --> [D], lexicon(D, det).  
noun --> [N], lexicon(N, noun).  
verb(Cat) --> [V], lexicon(V, verb, Cat).  
adj --> [A], lexicon(A, adj).  
  
{lexicon(take, verb, loc)}.  
{lexicon(get, verb, loc)}.  
{lexicon(put, verb, obj)}.  
{lexicon(place, verb, obj)}.  
  
{lexicon(to, prep, loc)}.  
{lexicon(from, prep, loc)}.  
{lexicon(on, prep, obj)}.  
{lexicon(in, prep, obj)}.
```

Question 8. Artificial Intelligence and Chess

[20 marks]

Making a computer that could play chess well was one of the early goals of Artificial Intelligence researchers. Computers can now play chess at grand master level, but it is not clear whether this involves intelligence. Explain why you think chess computers such as Deep Blue do, or do not, involve any intelligence, and whether creating chess computers contributes to our understanding of artificial intelligence.

□
