# Lecture 13-14: <br> Mid-trimester Recap, Animation started 

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## This week

Assignment 1 and mid-trimester test: Grades released Wednesday (please review), Assignment 2 due

## Today: Recap and Assignment 3

## Friday:

- Assignment 3 tutorial
- Assignment 2/3 helpdesk


## Recap: What is Computer Graphics?

## Creating new images using computers

May be created from:

- Existing images
- 3D models
- User strokes
- High dimensional data



## Recap: Areas in Computer Graphics

- Imaging = representing 2D images
- Modeling = representing 2D/3D objects
- Rendering = 2D images from 2D/3D models
- Animation = simulating changes over time



## Recap: Outline

Computer graphics: What you need to show other people your dreams.



- Specialized hardware - Graphics Processing Unit (GPU)
- API to interact with the hardware


## What is <br> OpenGL?

- Cross-platform
- Additional libraries:
- GLEW: extension
- GLFW: basic window with OpenGL rendering context
- Etc.
- Start with the classic OpenGL?


## Recap: Building Frameworks

- Integrated development environments (IDEs) on Windows, Mac, Linux and CMake tools



## Recap: Computer Graphics pipeline entities



## Recap: Geometry and Polygon Mesh

## - Face list

- Lists of coordinates
- Polygons are unrelated

- What are the nearest neighbor of a vertex ?
- What are the adjacent triangles of a vertex ?


## Phong Shading Model in OpenGL

- Phong illumination model is combination of
- Ambient $i_{\text {amb }}+$ Diffuse $i_{\text {diff }}+$ Specular terms $i_{\text {sepc }}$
- Developed by Bui Tuong Phong at Univ. Utah 1973

$$
\mathbf{I}=k_{a} i_{a}+k_{d} i_{d}(\mathbf{n} \bullet \mathbf{l})+k_{s} i_{s}(\mathbf{r} \bullet \mathbf{v})^{m_{s i d}}
$$

- $\mathrm{k}_{\mathrm{a}} \mathrm{k}_{\mathrm{d}} \mathrm{k}_{\mathrm{s}}$ are material properties having RGB components



## Transformations




## Stages of Vertex Transformations



## Surface Details



- How is it even possible to make it look things look like they are moving, or even alive with the computer?


Image credit: https://giphy.com/gifs/animated-loop-walking-XGnWMiVXL87Xa

## Object interaction: Bounding box/volume


https://www.are.na/tetlie/boundingbox https://en.wikibooks.org/wiki/OpenGL_Progra mming/Bounding box

## Boids

simulation animation

emergent behaviour
vector algebra



## Our inspiration

- National Geogiraphic fight of the starlings
https://www.youtube.com/watch?v=V4f_1 r80RY
- A murmuration of starlings


## Real flocks of birds \& schools of fish

- Upper bound limited only by actual population
- Starlings: flock of I.5 million birds
- Herring: school of hundreds of millions covering dozens of square kilometres
- Localized reasoning must be used
- A bird/fish only knows about its nearest neighbours

http://thefishbowInetwork.com/blog/wp-content/uploads/20|3/I0/school-free-of-fish.jpg


## Why go to school?

- Socialization
- Reproduction
- Protection from predators
- Foraging for food is quicker


## Simulating flocking: Boids

- Early work by Reynolds
- SIGGRAPH I987
- Boid: a member of the flock

- Key idea: local rules produce emergent behaviour giving believable-looking flocking
- Original Boids video by Reynolds https://www.youtube.com/watch?v=86iQiV3-3IA Notice the very simple quality of the graphics, generated on one of the fastest computers at the time.
- The first use of simulated flocking in a movie was Batman Returns (I992). It used a modified version of the original boids software to simulate
- bat swarms https://www.youtube.com/watch?v=jCVwdeAobYc
- penguin flocks
https://www.youtube.com/watch?v=APs3qbAEIFY
- The Lion King (I994) included a wildebeest stampede where a boids-like simulation was the only sane way in which to produce the effect of hundreds of animals charging down a gorge in a realistic manner https://www.youtube.com/watch?v=XM_VHtSDMIQ
- Orcs march on Minas Tirith https://www.youtube.com/watch?v=bPhIKXA8egU


## Reynolds' rules

- Avoidance
- Alignment
- Cohesion



## How do boids work?

- A Flocking Simulation https://www.youtube.com/watch?v=QbUPfMXXQIY


## Avoidance

- Boids avoid crashes

- Each boid looks at the flock mates in its neighbourhood and applies a force to push it away from its neighbours

Alignment

- Boids want to fly in the same direction

- Each boid looks at the flock mates in its neighborhood and applies a force to line it up with the average direction of its neighbours


## Cohesion

- Boids want to be near their flock mates

- Each boid looks at the flock mates in its neighborhood and applies a force to move towards the average position of its neighbours


## Representing a boid

- A boid has
- A position $\quad \mathbf{x}=\left[\begin{array}{l}x \\ y \\ z\end{array}\right]$
- Velocity

$$
\mathbf{v}=\left[\begin{array}{l}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]
$$



## Updating a boid's position

- Add velocity (times the time-step) to position

$$
\begin{aligned}
& \mathbf{x}_{\text {new }}=\mathbf{x}+(\mathbf{v} \times h) \\
& x_{\text {new }}=x+\left(v_{x} \times h\right) \\
& y_{\text {new }}=y+\left(v_{y} \times h\right) \\
& z_{\text {new }}=z+\left(v_{z} \times h\right)
\end{aligned}
$$



- $h$ is the time-step (scalar)


## How do the forces work?


$\mathbf{x}_{\text {new }}=\mathbf{x}+(\mathbf{v} \times h)$ - Position is updated by velocity $\mathbf{v}_{\text {new }}=\mathbf{v}+(\mathbf{a} \times h) ■$ Velocity is updated by acceleration $\mathbf{a}=\mathbf{f} / \mathrm{m} \quad$ - Acceleration is force/mass

## Cohesion



- Find the centroid of the neighbours' positions

$$
\mathbf{x}_{c}=\sum_{j \in N(i)} \mathbf{x}_{j} /|N(i)|
$$

- Create a force that goes from your position to the centroid

$$
\mathbf{f}_{x}=k_{x}\left(\mathbf{x}_{c}-\mathbf{x}_{i}\right)
$$

Who are the boids
in your neighbourhood?

- We specify a distance $d$ that a boid can "see"
- We check all other boids to see if they are within distance $d$

$$
N(i)=\left\{j: j \neq i \wedge\left|\mathbf{x}_{j}-\mathbf{x}_{i}\right|<d\right\}
$$

## Alignment



- Find the average of the neighbours' velocities

$$
\mathbf{v}_{c}=\sum_{j \in N(i)} \mathbf{v}_{j} /|N(i)|
$$

- Create a force that adjusts the boid's velocity to be closer to the average speed

$$
\mathbf{f}_{v}=k_{v}\left(\mathbf{v}_{c}-\mathbf{v}_{i}\right)
$$

## Avoidance



$$
\mathbf{f}_{a}=k_{a} \overbrace{i}^{\sum_{j \in N(i)}} \frac{1}{\mid \underbrace{}_{3}} \frac{1}{\left|x_{i}-x_{j}\right|} \frac{\left(x_{i}-x_{j}\right)}{\mid \underbrace{\left|x_{i}-x_{j}\right|}_{2}}
$$

1 For each boid in the neighbourhood create a force that
2 pushes away from the boid,
3 weighted by the inverse of the distance,
4 add all these forces together


## Applying those forces

- Add up the forces and divide by the boid's mass

$$
\mathbf{a}=\left(\mathbf{f}_{x}+\mathbf{f}_{v}+\mathbf{f}_{a}\right) / m
$$



- Update velocity

$$
\mathbf{v}_{\text {new }}=\mathbf{v}+(\mathbf{a} \times h)
$$



- Update position

$$
\mathbf{x}_{\text {new }}=\mathbf{x}+(\mathbf{v} \times h)
$$



## What operations make sense?

- vector $=$ vector + vector
- vector $=$ vector - vector

- vector $=$ scalar $\times$ vector
- vector $=$ point - point
- point $=$ point + vector
- point $=$ point - vector
- point = average of points


$$
\mathbf{x}_{c}=\sum_{j \in N(i)} \mathbf{x}_{j} /|N(i)|
$$

## Must update all boids together

First calculate forces for all boids

## Then update velocity and position for all boids

## What they don't usually tell you

- Need to balance forces carefully (experiment)
- Careful choice of $k_{x}, k_{v}, k_{a}$
- Mass is an arbitrary number
- If all boids weigh the same, can pretend that $m=1$
- Need to limit speed and force
- Enforce a maximum speed and a maximum force
- Apply maximum force limit to each force individually


## How do I limit a vector?

## Limiting a scalar

if $f>\max$
then $f_{\text {new }}=\max$

Limiting a vector
if $|\mathbf{f}|>\max$
then $\mathbf{f}_{\text {new }}=\max \times \frac{\mathbf{f}}{|\mathbf{f}|}$

## What else haven't you told me?

- You need to stop the boids from flying off into the distance
- Define an axis-aligned box to keep the boids in and then:

Force or Bounce or Wrap


